



Mark Scheme (Results)

Summer 2021

Pearson Edexcel International Advanced Level
In Statistics S2 Paper WST02/01

Question Number	Scheme	Marks						
Throughout the paper the candidates may use different letters to the ones given in the mark scheme.								
1.	<p>(a) [$X \sim$ the number of pansy seeds that do not germinate or $Y =$ the number...that <u>do</u> germinate] $X \sim B(20, 0.05)$ <u>or</u> $Y \sim B(20, 0.95)$</p> <p>(i) $P(X \leq 4) - P(X \leq 2) = 0.9974 - 0.9245$ <u>or</u> $\binom{20}{3} 0.05^3 \times 0.95^{17} + \binom{20}{4} 0.05^4 \times 0.95^{16} = 0.05958... + 0.01332...$ $= 0.072909...$ awrt 0.0729</p> <p>(ii) $P(X \leq 1)$ <u>or</u> $P(Y \geq 19) = 20 \times (0.95)^{19} (0.05) + (0.95)^{20}$ $= 0.7358$ <u>or</u> $= 0.735839...$ awrt 0.736</p> <p>(b) [Let $W =$ no. of packets where $Y > 18$] $P(W = 5) = ("0.7358...")^5$ $= 0.21573...$ awrt 0.216</p> <p>(c) $H_0 : p = 0.05$ $H_1 : p > 0.05$</p> <p>(d) [$V =$ no. of seeds that do not germinate $V \sim B(100, 0.05)$ approximates to] $V \sim Po(5)$</p> <table border="1" style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th style="width: 33%;"></th> <th style="width: 33%;">CR for 1-tail in (c)</th> <th style="width: 33%;">CR for 2-tail in (c)</th> </tr> </thead> <tbody> <tr> <td>$P(V \geq 8) = 1 - P(V \leq 7)$ $= 1 - 0.8666$ $= 0.1334$</td> <td>$P(V \geq 9) = 0.0681$ $P(V \geq 10) = 0.0318$ CR $V \geq 10$ oe</td> <td>$P(V \geq 10) = 0.0318$ $P(V \geq 11) = 0.0137$ CR $V \geq 11$ oe</td> </tr> </tbody> </table> <p>Accept H_0 <u>or</u> not significant <u>or</u> 8 does not lie in the critical region Data consistent with Spany's claim <u>or</u> Insufficient evidence for Jem's belief <u>or</u> insufficient evidence that percentage of seeds not germinating is more than 5% (o.e.)</p>		CR for 1-tail in (c)	CR for 2-tail in (c)	$P(V \geq 8) = 1 - P(V \leq 7)$ $= 1 - 0.8666$ $= 0.1334$	$P(V \geq 9) = 0.0681$ $P(V \geq 10) = 0.0318$ CR $V \geq 10$ oe	$P(V \geq 10) = 0.0318$ $P(V \geq 11) = 0.0137$ CR $V \geq 11$ oe	<p>B1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1 (5)</p> <p>M1</p> <p>A1 (2)</p> <p>B1</p> <p>(1)</p> <p>M1A1</p> <p>M1</p> <p>A1</p> <p>dM1</p> <p>A1cso</p> <p>(6)</p> <p>Total 14</p>
	CR for 1-tail in (c)	CR for 2-tail in (c)						
$P(V \geq 8) = 1 - P(V \leq 7)$ $= 1 - 0.8666$ $= 0.1334$	$P(V \geq 9) = 0.0681$ $P(V \geq 10) = 0.0318$ CR $V \geq 10$ oe	$P(V \geq 10) = 0.0318$ $P(V \geq 11) = 0.0137$ CR $V \geq 11$ oe						
Notes								
(a)	B1: writing or using $B(20, 0.05)$ [Allow $Y \sim B(20, 0.95)$ if Y is clearly defined]. Implied by 1 correct prob.							
(i)	M1: for $P(X \leq 4) - P(X \leq 2)$ <u>and</u> one correct prob. <u>or</u> $P(X = 3) + P(X = 4)$ <u>and</u> 1 correct prob.							
(ii)	M1: for $P(X \leq 1)$ <u>or</u> $[20] \times (0.95)^{19} (0.05) + (0.95)^{20}$ - condone missing 20							
(b)	M1: for (their(a)(ii)) ⁵							
(c)	B1: both hypotheses correct with p or π							
(d)	<p>1st M1: for realising a Poisson approximation is appropriate. NB $Po(95)$ is M0A0</p> <p>1st A1: writing or using $V \sim Po(5)$ i.e correct mean for the Poisson.</p> <p>2nd M1: for writing or using $1 - P(V \leq 7)$ <u>or</u> $P(V \leq 7) = 0.8666$ <u>or</u> writing $P(V \geq 10) = 0.0318$ <u>or</u> $P(V \geq 9) = 0.0681$ <u>or</u> $P(V \geq 11) = 0.0137$ leading to a CR. Implied by correct CR <u>or</u> probability = awrt 0.133</p> <p>2nd A1: for awrt 0.133 <u>or</u> $V \geq 10$ oe (e.g. $V > 9$) <u>or</u> $V \geq 11$ oe allow any letter but CR must match part(c)</p> <p>3rd dM1: dep on 2nd M1. ft their CR or probability. A correct statement based on comparing 8 with their CR <u>or</u> their prob with 0.05 or 0.025 [condone $0.866 < 0.95$]– contradicting non-contextual comments M0</p> <p>3rd A1 cso: all previous marks must be awarded. A correct statement in context. Need Bold words. NB award M1A1 for a correct contextual statement on its own. If there are no hypotheses or they are the wrong way around, then 3rd M0 3rd A0</p> <p>Normal approximation: Award marks in pairs with 2, 4 or 6 marks available</p>							
SC1	Sight of $N(5 \text{ or } 95, \sqrt{4.75^2})$ M1A1; probability awrt 0.125/6 M1A1; Correct contextual concl' dM1A1							
SC2	No approximation: Use of $B(100, 0.05)$ M0A0; probability awrt 0.128 <u>or</u> CR ≥ 10 M1A1; then M0A0							

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<p>2. (a)</p> <p>(b)</p> <p>(c)</p> <p>(d)</p> <p>(e)</p>	<p>[$X =$ number of faults in 4 m^2 so $X \sim \text{Po}(3)$]</p> <p>$P(X = 5) = P(X \leq 5) - P(X \leq 4) [= 0.9161 - 0.8153]$ <u>or</u> $\frac{e^{-3}3^5}{5!}$ (allow λ instead of 3)</p> <p>$= 0.1008$ <u>or</u> $0.100818\dots$ awrt 0.101</p> <p>[$Y =$ number of faults in 6 m^2 so] $Y \sim \text{Po}(4.5)$ <u>and</u> $[P(Y > 5)] = 1 - P(Y \leq 5) [= 1 - 0.7029]$</p> <p>$= 0.2971$ <u>or</u> (calc) $0.29706956\dots$ awrt 0.297</p> <p>0.101 (or ft their answer to (a))</p> <p>Faults occur independently/ randomly</p> <p>[$F =$ number of faults in a small rug] $F \sim \text{Po}(0.9)$</p> <p>$e^{-0.9n}n \times 80 + (1 - e^{-0.9n})n \times 60 \geq 4000$ <u>or</u> (awrt 0.407)$n \times 80 +$ (awrt 0.593)$n \times 60 \geq 4000$</p> <p>$n \geq \frac{4000}{20e^{-0.9n} + 60} = 58.71\dots$</p> <p>$n = \underline{59}$</p> <p>$H_0 : \lambda = 9$ $H_1 : \lambda > 9$</p> <p>$R \sim \text{Po}(0.9 \times 10)$ <u>and</u> $[P(R \geq 13)] = 1 - P(R \leq 12) [= 1 - 0.8758]$</p> <p>$P(R \leq 13) = 0.9261$ <u>or</u> $P(R \geq 14) = 0.0739$ <u>or</u> $P(R \leq 14) = 0.9585$ <u>or</u> $P(R \geq 15) = 0.0415$</p> <p>$[P(R \geq 13)] = 0.1242$ awrt 0.124 <u>or</u> CR $R \geq 15$ (oe)</p> <p>so insufficient evidence to reject H_0 /not significant/ not in critical region</p> <p>There is insufficient evidence that the rate at which faults occur is higher for Rhiannon</p>	<p>M1</p> <p>A1</p> <p>(2)</p> <p>M1</p> <p>A1</p> <p>(2)</p> <p>B1ft</p> <p>B1</p> <p>(2)</p> <p>B1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>(4)</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>(5)</p> <p>Total 15</p>
Notes		
<p>(a)</p> <p>(b)</p> <p>(c)</p> <p>(d)</p> <p>(e)</p>	<p>M1: for using or writing $P(X \leq 5) - P(X \leq 4)$ <u>or</u> $\frac{e^{-\lambda}\lambda^5}{5!}$ (Accept letter λ or any value of λ)</p> <p>M1: writing or using $\text{Po}(4.5)$ <u>and</u> sight of $[P(Y > 5)] = 1 - P(Y \leq 5)$ Implied by sight of $1 - 0.7029$</p> <p>2nd B1: for a comment about faults occurring randomly/independently <u>or</u> Poisson has “no memory”</p> <p>B1: writing or using $\text{Po}(0.9)$ May be implied by sight of 0.407 or 0.593</p> <p>1st M1: for $e^{-\lambda}n \times 80 + (1 - e^{-\lambda})n \times 60 > 4000$ any value for λ. Allow = 4000</p> <p>2nd M1: for solving their equation leading to a positive value of n. Allow any value of λ and allow $n = \dots$</p> <p>A1: for an answer of 59 only</p> <p>B1: both hypotheses correct with λ or μ. Allow 3 or 0.75 or 0.9 instead of 9</p> <p>1st M1: for writing or using $\text{Po}(\text{“}9\text{”})$ and writing or using $1 - P(R \leq 12)$ (implied by $1 - 0.8758$) <u>or</u> one of: $P(R \leq 13) = 0.9261$, $P(R \geq 14) = 0.0739$, $P(R \leq 14) = 0.9585$, $P(R \geq 15) = 0.0415$ leading to a CR</p> <p>1st A1: for probability = awrt 0.124 <u>or</u> CR of $R \geq 15$ oe e.g. $R > 14$</p> <p>2nd M1: for a correct conclusion based on their prob & 0.05 <u>or</u> their CR & 13. Assume correct hypotheses. Do not allow contradicting conclusions</p> <p>2nd A1: dep on both Ms for a correct contextual comment including the words in bold.</p>	

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<p>4.</p> <p>(i)</p> <p>(ii)</p>	<p>[A = the number on the ball] $P(A=1)=\frac{2}{9}$ $P(A=2)=\frac{1}{3}$ $P(A=5)=\frac{4}{9}$</p> <p>Possible samples with a range of 4 are: (1,1,5) (1,2,5) (1,5,5)</p> <p>(1,1,5) $\frac{2}{9} \times \frac{2}{9} \times \frac{4}{9} \times 3 = \frac{16}{243}$ <u>or</u> (1,5,5) $\frac{2}{9} \times \frac{4}{9} \times \frac{4}{9} \times 3 = \frac{32}{243}$</p> <p>(1,2,5) $\frac{2}{9} \times \frac{1}{3} \times \frac{4}{9} \times 6 = \frac{16}{81}$</p> <p>$P(B=4) = \frac{16}{243} + \frac{32}{243} + \frac{16}{81} = \frac{32}{81}$</p> <p>$P(B=0) = \left(\frac{2}{9}\right)^3 + \left(\frac{1}{3}\right)^3 + \left(\frac{4}{9}\right)^3 = \frac{11}{81}$</p> <p>$P(B=1) = 3 \times \frac{2}{9} \times \left(\frac{1}{3}\right)^2 + 3 \times \frac{1}{3} \times \left(\frac{2}{9}\right)^2 = \frac{10}{81}$ <u>or</u> $P(B=3) = 3 \times \frac{1}{3} \times \left(\frac{4}{9}\right)^2 + 3 \times \frac{4}{9} \times \left(\frac{1}{3}\right)^2 = \frac{28}{81}$</p> <p>$1 - \frac{11}{81} - \frac{10}{81} - \frac{32}{81} = \frac{28}{81}$ <u>or</u> $1 - \frac{11}{81} - \frac{28}{81} - \frac{32}{81} = \frac{10}{81}$</p> <table border="1" data-bbox="240 891 1369 1003"> <tr> <td><i>b</i></td> <td>0</td> <td>1</td> <td>3</td> <td>4</td> </tr> <tr> <td>$P(B=b)$</td> <td>$\frac{11}{81}$</td> <td>$\frac{10}{81}$</td> <td>$\frac{28}{81}$</td> <td>$\frac{32}{81}$</td> </tr> </table>	<i>b</i>	0	1	3	4	$P(B=b)$	$\frac{11}{81}$	$\frac{10}{81}$	$\frac{28}{81}$	$\frac{32}{81}$	<p>B1</p> <p>M1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>M1</p> <p>M1</p> <p>B1</p> <p>A1</p> <p>(10)</p> <p>Total 10</p>
<i>b</i>	0	1	3	4								
$P(B=b)$	$\frac{11}{81}$	$\frac{10}{81}$	$\frac{28}{81}$	$\frac{32}{81}$								
Notes												
<p>(i)</p> <p>(ii)</p> <p>SC A0 in (i)</p>	<p>B1: for writing or using the 3 correct probabilities</p> <p>1st M1: for identifying the 3 possible samples</p> <p>2nd M1: for $p \times p \times q \times 3$ <u>or</u> $p \times q \times q \times 3$ where p and q are probabilities with $(p + q) < 1$</p> <p>3rd M1: for $p \times q \times r \times 6$ where p, q and r are probabilities with $(p + q + r) = 1$</p> <p>A1: for $\frac{32}{81}$ <u>or</u> awrt 0.395 [Calc: 0.3950617...]</p> <p>1st M1: for $p^3 + q^3 + r^3$ (for their p, q and r)</p> <p>2nd M1: for $3 \times p \times (q)^2 + 3 \times q \times (p)^2$ <u>or</u> $3 \times q \times (r)^2 + 3 \times r \times (q)^2$ (for their p, q and r)</p> <p>3rd M1: for use of all probabilities of $P(B=b)$ adding to 1 [Must have 3, 4 or 5 values for b]</p> <p>B1: for ranges 0, 1, 3 and 4 with none omitted and no extras. Allow extras if assigned probability of 0</p> <p>A1: for a fully correct probability distribution.</p> <p>If A0 scored in (i) <u>and</u> all other marks scored in (ii) <u>and</u> correct prob's for 2 values of b : award A1 in (ii)</p>											

Question Number	Scheme	Marks
<p>5 (a)(i)</p> <p>(ii)</p> <p>(b)</p> <p>(c)</p> <p>(d)</p>	<p>If $y = 0$ then $1 - (\alpha + \beta y^2) = 0 \quad \therefore \alpha = 1$ *</p> <p>If $y = 5$ then $1 - (\alpha + \beta y^2) = 1$</p> $1 + 25\beta = 0 \quad \therefore \beta = -\frac{1}{25} \quad *$ <p>$F(y) = \frac{1}{25}y^2$ so $f(y) = \frac{dF(y)}{dy} = \frac{2}{25}y$</p> $\therefore [f(y) =] \begin{cases} \frac{2}{25}y & 0 \leq y \leq 5 \\ 0 & \text{otherwise} \end{cases}$ <p>$\left[P\left(R > \frac{11}{5}\right) = P\left(Y > \frac{5}{3}\right) = 1 - \frac{1}{25} \times \left(\frac{5}{3}\right)^2 = \right] \frac{8}{9}$ oe</p> <p>$\frac{3d - \frac{11}{5}}{3d - d} = \frac{8}{9}$ oe or $\frac{\frac{11}{5} - d}{3d - d} = \frac{1}{9}$ oe</p> $d = \frac{9}{5}$ oe <p>$P\left(Y < \frac{11}{5}\right) = \frac{121}{625}$ or 0.1936</p> <p>[Let G = the number of spins with distance < 2.2 m]</p> <p>[$P(G \geq 5) =$</p> $\left(\frac{1}{9}\right)^3 \times \left(\frac{121}{625}\right)^3 + 3 \times \left(\frac{1}{9}\right)^2 \times \left(\frac{8}{9}\right) \times \left(\frac{121}{625}\right)^3 + 3 \times \left(\frac{1}{9}\right) \times \left(\frac{121}{625}\right)^2 \times \left(\frac{504}{625}\right)$ <p>= 0.000 373226 awrt 0.000 373</p>	<p>B1cso</p> <p>B1cso</p> <p>(2)</p> <p>M1</p> <p>A1</p> <p>(2)</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>(3)</p> <p>B1</p> <p>M1, M1</p> <p>A1</p> <p>(4)</p> <p>Total 11</p>
Notes		
<p>(a) (i)</p> <p>(ii)</p> <p>(b)</p> <p>(c)</p> <p>(d)</p>	<p>B1: for stating or using the fact that when $y = 0$ then $\alpha + \beta y^2 = 1$</p> <p>B1: for stating or using that when $y = 5$ then $\alpha + \beta y^2 = 0$ and setting up the equation leading to $\beta = -\frac{1}{25}$</p> <p>M1: for differentiating. Implied by $\pm \frac{2}{25}y$ can fit their value of β</p> <p>A1: for a fully correct $f(y)$ defined for the whole range.</p> <p>B1: for using $F(y)$ and $\frac{5}{3}$ to find $P(Y > \frac{5}{3})$. Allow $\frac{8}{9}$ or any exact equivalent.</p> <p>M1: for LHS = p where $0 < p < 1$</p> <p>A1: for $\frac{9}{5}$ or any exact equivalent e.g. 1.8</p> <p>B1: for $\frac{121}{625}$ or awrt 0.194 This mark could be implied by a correct answer.</p> <p>1st M1: for $p^3q^3 + np^2(1-p)q^3 + np^3q^2(1-q)$ where p and q are probabilities and n is an integer > 0</p> <p>2nd M1: for $p^3q^3 + 3p^2(1-p)q^3 + 3p^3q^2(1-q)$ where p and q are probabilities.</p> <p>A1: for awrt 0.000 373</p>	

Question Number	Scheme	Marks
6. (i)	$z = 1.25$ $\frac{187.5 - \mu}{\sigma} = 1.25$ $187.5 - \mu = 1.25\sigma$ $\mu = 225p$ $\sigma = \sqrt{225p(1-p)}$ $(187.5 - 225p)^2 = (1.25)^2 \times 225p(1-p) \text{ or } (150 - 180p)^2 = 225p(1-p) \text{ (o.e.)}$ $\text{e.g. } 900(5 - 6p)^2 = 225(p - p^2) \Rightarrow 4(25 - 60p + 36p^2) = p - p^2$ <p>Leading to $145p^2 - 241p + 100 = 0^*$</p>	B1 M1 M1 A1 M1 M1 M1 A1* M1 A1 (10)
(ii)	$[(29p - 25)(5p - 4) = 0 \Rightarrow] \quad p = 0.8 \text{ or } p = \frac{25}{29} \text{ (accept: 0.862(0689...))}$ $[p =] \underline{0.8} \text{ because 0.862 gives a mean greater than 188 (oe)}$	M1 A1 (10)
Notes		
(i)	B1: for 1.25 or better (calculator gives: 1.25027...) 1st M1: for attempting to use a continuity correction i.e. for sight of 188 ± 0.5 2nd M1: for standardising using μ and σ or np and $\sqrt{np(1-p)}$ (Condone letter n or any integer > 0) 1st A1: for a correct equation with compatible signs, allow 1.250... If using a value for n it must be 225 3rd M1: for $\mu = 225p$ seen at any stage in the working. 4th M1: for $\sigma = \sqrt{225p(1-p)}$ seen at any stage in the working. Must be for σ not $\sigma^2 = 225p(1-p)$ 5th M1: for squaring to get a quadratic equation in p 2nd A1*: dep on all previous Ms and use of 1.25 (with correct sign) for at least 1 correct intermediate step from a correct quadratic equation e.g one of those in scheme for 5 th M1	
(ii)	M1: for solving the quadratic correctly—leading to $p = \dots$ or implied by 0.8 or awrt 0.862 A1: for 0.8 <u>and</u> a correct reason to eliminate 0.862	